





$$S_{w} = \int_{0}^{\frac{b}{2}} x_{2}(y) dy - \int_{0}^{\frac{b}{2}} x_{1}(y) dy$$

$$S_{w} = \int_{0}^{\frac{b}{2}} [C_{R}] + \tan(\Lambda_{le})y dy - \int_{0}^{\frac{b}{2}} \tan(\Lambda_{te})y dy$$

$$= C_{R} (b/2) + \tan(\Lambda_{le})/2 (b/2)^{2} - \tan(\Lambda_{te})/2 (b/2)^{2}$$

A Partially Re-Usable **Horizontal Take-off & Landing** Launch Vehicle

A Continuing Case Study



Wes Kelly

Triton Systems, LLC 17000 El Camino Real – Suite 210A Houston, TX 77058

University of Houston Clear Lake

Houston, TX

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Historically, reusable and expendable launch systems have experienced rising and falling tides, but also variations in approach.

Among reusable concepts, 1st stages combining aircraft and rocket features have been examined less often.

This case includes horizontal take-off and landing (HTOL) craft with wings and air breathing engines; transitioning to rocket propulsion occurs at subsonic speed (M<1) and stratospheric altitude.

Stage recovery comes after separation of an expendable upper stage at rocket shutdown and subsequent coast to apogee and descent – heading off ultimately to a runway.

The locally based Stellar J project examines this approach, addressing integration, performance, preliminary design, missions and markets.

Scalability of the concept is examined based on constraints of hardware and markets.

Several applications prove promising, the most immediate: deployment of small satellite constellations.

As design has matured, aero-thermal and structural studies have become more and more focused and hardware trades address the specifics of a design distinct in nature.



At American Institute of Aeronautics & Astronatics "Space 2007" convention in Long Beach, CA Then Aerospace Corporation CEO & President Dr. William Ballhaus gave the keynote address.

Reviewing launch system development since Sputnik & the direction US should take for the next 50 years, Ballhaus recommended:

A <u>partially</u> reusable launch vehicle, concentrating reusability in the 1st stage; A vehicle with wings, air-breathing jets as well as rocket engines; Flying frequently, responding rapidly and able to deploy different upper stages (expendable or reusable) allowing for flexible operations.

% Reusable vs. % Expendable Hardware



Unknown to Dr. Ballhaus Triton Systems, LLC was working to develop such a vehicle ... The Stellar-J >>



RBS has potential for more cost-effectiveness

But there was still one key difference...

Triton Systems, LLC Desk1Triton@aol.com



The Planning for Partially Re-Usable Launch Vehicles Was Based on Vertical Take Off



Shuttle derivative & upgrade studies of the 80s & 90s Included Liquid Rocket Boosters to replace existing Solid Rocket Boosters.

Beside expendable LRBs In late 1990s, work included Liquid Fly-Back Boosters with wings and reusable rocket engines, cruising back to launch site in final sub-sonic flight leg on jet engine power.

Booster power plants featured newly available long-life, high performance kerosene-LOX staged combustion engines. RD-180 and several alternates. were rated for numerous starts.



Liquid Fly-Back Booster concepts, systems and hardware Re-arranged and re-scaled result in the HTO reusable first stage (RFS) described. But the launch system need not weigh 2000 tons at liftoff.

Triton Systems, LLC Desk1Triton@aol.com

Long Standing REPRESENTATION

The Stellar-J employs horizontal take-off and landing from conventional airfields

Rocket transitions occurs at subsonic stratospheric cruise.

Vehicle climbs to rocket shutdown at ~150,000 feet & hypersonic velocity. Releasing upper stages carrying payloads to orbit,

The reusable first stage returns to land & refurbishment.





The concept scales for configurations from 35-350 tons take-off weight based on Available high performance reusable engines.

Market research shows the opportunity for the smallest initial investment & earliest returns: the small satellite market, payloads ~ 100-lbs to low earth orbit (LEO).

A standing backlog of ~500 small payloads has remained for decades awaiting launch opportunities with limited slots and market costs of \$20,000 per payload pound.





But is this Launch System а Unicorn? Or...

Is There Something There?



Composite Materials & TPS X-34 Nominal Flight Profile 40 r 10 300 r 2508 30 Mach 200 6 Altitude, 150 Analyzed α, 20 -Mach kft To Fly Like X-15 **But Never Flown** 100 Fig. 1 Artist's concept of the X-34 configuration in flight. 10F Coast 2 Altitude Burnout 50 Descent L-1011 carrier aircraft Launch Ascen 01 0E 500 1500 0 1000 Recovery Ignition after separation maneuver Landing Time, sec Runway **Note Feature** Down range landing WAG18D trajectory profile. Fig. 4 Fig. 2 Typical X-34 flight profile.



Shuttle Endeavour over Houston en route To Retirement 2012





Voici le modèle OK-GLI de la navette spatiale soviétique Bourane, exposée maintenant au musée technique Speyer situé en Allemagne.

> Space Shuttle & Buran Ultimately Launched from Pads Re-Entry at velocities 4 times >X-15



An HTOL with wings and air-breathing jet engines to return and re-fly the first stage makes sense if...

 The rocket engines are high performance, compact, reusable and economical (cheaper to reuse than to replace, a lifetime of 20 to 30 re-starts

Dependent on: $m_F/m_I = exp(-\Delta V/(g I_{SP}))$ for each rocket stage

 m_F : final mass before rocket burn m_I : initial mass prior to rocket burn

 ΔV : velocity change due to rocket burn (measured in empty space w/o drag

I_{sp}: Specific Impulse [(lbf thrust/ lb propellant/sec) units: seconds]

- The jet engines and wings pay their own way in combination with the performance of the rocket engines by reducing the burden of the rocket engines in flight to orbit and assisting in re-entry.
- The RDT&E (non-recurring) cost and the operating (recurring) costs are competitive.
- There are existing missions, markets and customers for such services.
- The vehicle is comparatively flexible or versatile enough to go after them.



Valentin Petrovich Glushko Валенти́н Петро́вич Глушко́ 1909-1989 Chief Designer RD-170 LOX Rich-Kerosene Staged Combustion Cycle Rocket Engine Chamber Pressure: 250 bar (Successor: Boris Gubanov)

Revolutionary Products Made Available in the US in the 1990s

Beside High Performance I_{SP} High Thrust to Weight

Engines Long-Lived



Nikolai Dmitriyevich Kuznetsov

Николай Дмитриевич Кузнецов 1911-1995 Chief Designer of NK-31, NK-33 LOX Rich Kerosene Staged Combustion Cycle Rocket Engine Chamber Pressure(s): ~90 & ~150 bar Vacuum Thrust ~ 90,000-lbf



PUMP FED STAGED COMBUSTION CYCLE (SEVERAL VARIATIONS)

Fuel-Cooled Nozzle Pre-Burners turn Turbines With "Unbalanced" Exhausts Run Propellant Pumps High Pressure Propellant Gas Mixes Headed to Combustion Chamber



If turbine exhausts were To be dumped overboard in separate exhaust, Combustion chamber Pressures ½ to 1/3 less.

Engine volumes increase Thrust to weight goes down Low altitude specific impulse decreases Due to exit pressure in expanded nozzle. What is our answer?...





It is our objective in sharing our experience in developing such a vehicle (The Stellar-J) to relate

- Why do this? Does such a vehicle fulfill any need? Are there any advantages? Based on what?
- The history of development of such vehicles from our perspective
- Basic ideas about our launch vehicle obtained
 - Derived from our experience with civil space programs
 - Some of our own characteristic approaches to the problem
- Market considerations and how we identified them
 - Customers or the Community of Users -Scalability and Matching Vehicle Variation with Potential Mission, Market and Resources
- Methods Used to develop the preliminary design
 - Launch simulations, Propulsion Analysis, Aerodynamics and Aero Data Bases
 - Structural Studies (In search of the Delta Wing)
- Advancing beyond Preliminary Design
 - Selecting components, partners, suppliers, contacting potential customers.

To relate the way we tie elements together: the effort at integration in design.





Stellar-J Elevator Presentation



The Small Satellite User Community

Needs an inexpensive , reliable, launch system that can

- Deploy satellites & turn around fast,
- Grow with user needs,
- Cultivate capabilities for the future such as:
- Rendezvous & Return Cargo

The size of the community, both domestic & foreign, is large:

- Small Companies
- Civil & Military Offices
- Private Research Institutes
- Universities & Related Research Consortia



Its backlog stands at hundreds of satellites in a \$20K/lbm payload market.

Our Approach:

Horizontal take and landing first stage with wings and jet engines.



Rocket burn from airline cruise to typical booster rocket staging.

Concept scales from 35 to 350 tons.. Capable of operating at conventional airfields up to jumbo jet facilities....

Stellar-J Launch System:

Horizontal take-off and landing 1st stage with wings & air-breathing engines Climbs to stratospheric subsonic cruise before igniting Rocket engines and ascent to hypersonic high altitude burn-out.

Turbofan flight portion removes ~2500 fps from the rocket equation (1 & 2) Requirement of ~30,000 fps ideal velocity to obtain orbital flight.

Recovering long-lived high- performance rocket engines & 1st stage elements allows:

- Order of magnitude reduction in first stage recurring costs (=> aircraft costs)
- Quick turn-around and frequent access to flight for payloads
- Self-ferrying capabilities and operation to & from air fields with facilities
- Flexible azimuth and inclination adjustments to launch windows
- Modular vehicle design adaptable to several markets (includes suborbital tourism).

Stellar-J Approach
Takes "Work"
Out of the
Rocket Equation

1. Velocity L	osses with	Altitude:		2. Azimuth Velocity	Work2 < Work1			
Altitude (ft)	~(2 g h) ^{0.5}	Velocity	(fps)	Contributed by Jet Flight	Constant	= mv² +	- mg h	
				0.7 - 0.9 M at altitude	TE3 (orbit)	= KE3	+ PE3 =	
10,000		802		< 1000-fps	TE2 (flight)	= KE2	+ PE2 + Work2	2
35,000		1,500			TF1 (ground) = KF1	+ PF1 + Work	1
350,000		< 4,745			(8,04,14	,	•••••••••	







Those are NOT our vehicles.

NASA Glen Research Center In 2011 was interested in Beamed Energy Propulsion.

Concepts were based on laser installations on the ground or in space focusing microwave, visible or infrared radiation on spacecraft mirrors or concentrators to provide propellant heating without combustion or nuclear energy.



 ΔR changes with $\beta(t) = \beta_{0} - \omega t$

ω angular rate effected by both orbital rate and Earth rotation



RESEARCH

What did that have to do with Stellar-J and Triton Systems?

Triton working as a Subcontractor with the Orbital Technologies team on

NASA Research and Technologies Contract for Aerospace Propulsion Systems (RTAPS)

researched beam energy and examined how Stellar-J Vehicle could be applied

...???

Out of Plane Spacecraft and Rotating Earth, Initially Circular Orbit

- X₁ = Beamed Power Ground Site
- \underline{X}_2 = Orbiting Spacecraft (assumed circular (initially)
- $\underline{X}_1 \circ \underline{X}_2 / |X_1| |X_2| = (x_1x_2 + y_1y_2 + z_1z_2) / [R_0(R_0 + H)]$
- $\underline{X}_{1} = R_{0} \left(\cos \alpha_{R1} \cos \delta_{R1} , \sin \alpha_{R1} , \cos \delta_{R1} , \sin \delta_{R1} \right)$
 - = $R_0 (\cos \lambda (t) \cos \phi E, \sin \lambda(t) \cos \phi_E, \sin \phi_E)$ where $\lambda = \lambda_0 + \omega_E t$
- $\underline{X}_2 = (R_0 + H) (\cos \alpha_{R2} \cos \delta_{R2}, \sin \alpha_{R2}, \cos \delta_{R2}, \sin \delta_{R2})$
 - = $(R_0 + H) (\cos\Omega \cos\theta^* \sin\Omega \cos i \sin\theta^*, \sin\Omega \cos\theta^* + \cos\Omega \cos i s\theta^*, \sin i \sin\theta^*)$
- α_R , δ_R : celestial coordinates right ascension and declination for unit vectors 1 and 2.
- i: inclination
- Ω: ascending node, corresponding to right ascension position of orbit crossing northward
- θ*: for circular orbit, great circle arc from ascending node





RESEARCH



Whether laser beam source in space or on the ground geometric constraints & attenuation affect power delivery.

For ground-based case, orbital window limited by overflight & nodal regression.

But on ascent, activity is also geographically limited. Could beamed energy power an upper stage? Upper Stage Ascent Profiles High & Low ("Demo) Energy RLV First Stage Ascents Single and 2-Stage Expendables Higher Specifc Impulse (CH4) Lofts ascent flight path.

Nominal RLV Stage Demonstrator RLV Stage Demonstrator 2-stage Expendable Nominal Single Expendable Upper Nominal 2-Stage Expendable LCH4 –fueled 2nd Stage

Beamed Energy Constant Thrust Upper Stage Time-Altitude Profiles Compared to Nominal Chemical Engines 350, 400, 450-sec Specific Impulse . Beamed Energy Cases: 500, 600, 800-secs.



Vs 300 to 450), buthow much power is needed for equivalence in thrust to a chemical engine?

RESEARCH

Specific impulse (ISP)

could be higher than

(500 to 800 seconds

Chemical systems





300

200

0

500

1000

1500

time (seconds)

2000

2500

3000

n.mi.. 100

1st Stage winged RLV (Reusable Launch Vehicle) Flies out from launch site, deploys expendable upper stages with terminal stage flying over G/S beam energy site.

RESEARCH



Table 1.3 Stel Actual I	lar-J Ter Payloads	minal We To Be De	eights Ba termined	sed on 2 Based	2 nd Stage S on Stage	Scaling : Mass Fi	and Is ractio	sp Variations n λ _{stage2}	s
$m_{IIA} + m_{IIB} + m_{PL}$ Sepa	aration W	eight: 12	,000-lbs	m _{IIB} =	4160-lbs	Thrust	= 261	0-lbf	
I _{SP} : Final: Power:	320 1602	350 1772	400 1929	450 2095	500 2238 56.9	600 2478 68.3	80 281 91.1	0-secs 1-lbm L-MW	RESEARCH
m _{IIA} + m _{IIB} + m _{PL} Separation Weight: 4,000-lbs m _{IIB} = 1386-lbs Thrust = 870								For various thrust and specific impulse levels	
I _{SP} : Final: Power:	320 534	350 590	400 643	450 698	500 746 19.0	600 826 22.7	80 93 30.	0-secs 7-lbm 4-MW	equivalent megawatt Full efficiency power,
Stage IIB I _{SP} (secs):	32	0	350		400-450	500-	800		Power received at the spacecraft
Fuel & Oxidizer	Keros	sene-LOX	CH4-L	OX	LH2- LO	X LH2	2		in blue bold .
Chemical Combustion	on X	(Х		Х				Receiver technology: TBD
Beamed Energy							X		

The preceding account is a "research anecdote" about examining a new vehicle concept.

But it demonstrates possibilities for the launch system based on its versatility and potential adaptability:

- Capability of launch from a runway and flight out to various headings or azimuths. This not only allows acquisition of various orbital inclinations and ability to match tracks for rendezvous, it also allows over flight over specific geographic features.
- 2. The expendable upper stage system base-lined as 2-stages (IIA & IIB) provides a simple common boost element (IIA) and an adaptable mission oriented terminal stage (IIB) trading propellant, payload and bus features.

We will talk more about other features in the following sections.



Subsequent material from presentations Will be re-examined from an instructional perspective.

Sequence

Computer Tools: Some Discussion about means developed to obtain initial analyses.

Computer Output in Plots: Vehicle Characteristic Behaviors and Variations

Vehicle Layout: Moving out in all directions from examinations of simple trajectories elaborating on

- mass properties and transformations in phases of flight
- aero and thermodynamics,
- control systems (flaps and thrusters) and stability analysis
- materials responding to stress and stain
- hardware selections such as jet engines...

Accommodating Missions and Markets (Optional/Questions)

Establishing Criteria for Trades









Program to Optimize Simulated Trajectories II (POST2)

Home

The Program to Optimize Simulated Trajectories II (POST2) is a generalized point mass, discrete parameter targeting and optimization program. POST2 provides the capability to target and optimize point mass trajectories for multiple powered or unpowered vehicles near an arbitrary rotating, oblate planet. POST2 has been used successfully to solve a wide variety of atmospheric ascent and entry problems, as well as exoatmospheric orbital transfer problems. The generality of the program is evidenced by its multiple phase simulation capability which features generalized planet and vehicle models. This flexible simulation capability is augmented by an efficient discrete parameter optimization capability that includes equality and inequality constraints. POST2 supports NASA's Strategic Goal to expand the frontiers of knowledge, capability, and opportunity in space by directly contributing to expanding our human and robotic presence into the solar system and to the surface of Mars as well as other planetary bodies.

Others

- SORT: Space Optimization of Rocket Trajectories
- OTIS: Optimization of Trajectories by Implicit Simulation...



SVDS: (Historical: Shuttle Vehicle Dynamic Simulation: 6DOF & GN&C)

We developed a family of our own: LAUNCH, AEXTRAP... (Progenitors for ballistic launch, orbital finite burns, propulsion trades)

JETFJ... 1, 2, 3, ... 6, 7 - Working tools for HTOL with wings & jet engines

Trajectory Simulations Concentrate on Paths, Not Design.

Ascent Simulations: Numerical Integration & Optimization Methods, Largely for 2-Point Boundary Problems.

Simulations with Rocket & Jet Engines (with wings) grew Up in separate homes.



F:\AI9112~1\JETFJ17.EXE	
? 1. First data case is default. Enter # to select subsequent cases. iconf, wgtØi, tmagi, neng, cisp, vex, S, akf tmagrk, cispv, cispsl, wjetf, rprop, ustwgt, isp, thrst toffjt, tonrk, toffrk, pitrtc, pitchi, alphae, nrock iiab , fuel 1-3, clm2ai, clm2bi, uisp2bi, thrs2bi, paylodi, xmri1, xmri2, xmri3 icode, wingldi, Wareai, clmbLEi, clmBTEi, hspani cti, cri, ctcr	Representations of Nominal Trajectories
Nominal 1NK-31, 2BMR710s, Upper Stage, 27200.00 $L/D = 5.91$ 168000.020000.027200.001094.001.000090000.0335.00278.548000.036000.012000.0300.09600.01350.01300.01435.0.10018.045.01121.8500.8917320.001305.00300.002.601.60142.001639.0045.00.00420.0072.00490.00.0000	PLOT VARIABLES PLOT 1 Time (seconds) 2 Altitude (feet) 5 Gam Rel. (deg) 6 Alpha 9 Down Range (nmi) 10 Jet thrust(h,v) 1 12 Lift accol 1
Nominal 1 NK-31, 2 BMR710s, Upper Stage, $L/D = 5.91$ 2 68000.0 20000.0 2 7200.00 2500.00 1094.00 1.0000 90000.0 335.00 278.54 8000.0 36000.0 6000.0 300.0 4800.0 1350.0 1300.0 1435.0 .100 18.0 45.0 1 1 1 2 1 .8500 .8917 320.00 1305.00 300.00 2.60 1.60 2.20 1 42.00 1639.00 45.00 .00 420.00 72.00 490.00 .0000 ? _	VARIABLES13 Lift accel.14 Drag accel17 Wgt per SFC18 Wdot (lb/sec)121 Q-bar (lb/ft**2)22 Q*alpha25 sensed accel26 sens acc. dir.29 x (ft)30 y (ft)33 ydot (fps)34 zdot (fps)37 Temp adia wall38 Temp (R) amb41 Qload tot42 Elevator deflect45 Cm(M,alpha,cg)46 Cl (mach,alpha)49 al(3)50 Wingload lb/ft*2
<pre>? Trajectory Initial, Intermediate & Terminal Conditions Event Time Altitude Vrel Gamma Vinert Weight Latitude Az Alph Take-Off: 0. 100. 311.3 .000 1645.9 68000.0 29.00 90.0 10.5 10,000 ft: 481. 10005. 949.2 1.707 2284.4 67213.9 29.00 90.0 3.2 35,000 ft: 1168. 35015. 806.0 3.178 2142.9 66462.9 29.00 90.0 6.0 Ignition: 1300. 40924. 703.7 3.583 2041.0 66362.7 29.00 90.0 8.7 Shut-down: 1390. 106941. 3757.3 22.797 5098.7 42365.9 29.00 90.0 4.1 Apogee : 1464. 165391. 2902.8 .216 4247.9 32343.5 29.00 90.0 27.2 NZ max : 1302. 41138. 763.8 6.784 2101.0 65756.0 29.00 90.0 9.1 25k Start: 2700. 25005. 962.9 1.325 2299.1 32063.0 29.00 90.0 1.8 T-final : 3400. 46840. 936.7 2.599 2274.3 31535.8 29.00 90.0 3.0</pre>	<
Additional Minima and MaximaQmax:115.1189.964.41.0182299.167777.429.0090.02.9Qmax burn:1343.58756.2011.419.9093349.754724.729.0090.02.3Qmx entry:1390.108393.3738.422.8255079.942097.229.0090.04.2qdot up:1389.106941.3757.322.7975098.742365.929.0090.04.1qdot down:1520.135450.2819.5-18.1484162.832343.529.0090.025.0?MECO state initiates upper stage sequence.	43 cg in flight 44 Cm (mach,alpha) 47 al(1) 48 al(2) 51 p ambient









For the 1st Stage winged, reusable component of the Stellar-J, climb-out from subsonic stratospheric flight under rocket power exerts both mechanical & thermal loads.

Mechanical loads gather near the wing roots (discussed elsewhere).

Thermal loads concentrate at leading edges and tips.

Results for Thin Surfaces:



Upper & lower tip chord leading edges of wings vertical tails and winglets subject to highest Temperatures at highest Thermal fluxes dq/dt (BTU/sec/ft2).

Upper Stage Separation Wgts Based on a nominal value.

Margin Dependent on Wing Design



Performance Envelope Analysis: Altitude, Q, Velocity, Mach

4












Triton Systems LLC Houston TX 77058 281 286-3680





Nominal Stellar-J Selection (+ Trades)







lars for NACA 64-208 (naca64208-il)

Plot	Airfoil	Reynolds #	Ncrit	Max CI/Cd
	naca64208-il	50,000	9	26.6 at α=4.5°
~	naca64208-il	100,000	9	45.3 at α=3.75°
	naca64208-il	100,000	5	42.8 at α=3.5°
	naca64208-il	200,000	9	58.9 at α=3.25°
	naca64208-il	200,000	5	53.3 at α=3°
	naca64208-il	500,000	9	75.8 at α=2.75°
	naca64208-il	500,000	5	60.7 at α=2.5°
	naca64208-il	1,000,000	9	80.8 at α=2.25°
	naca64208-il	1,000,000	5	70.1 at α=5°
Upo	date plots	Reynolds number	calculate	<u>21</u>



Component Weights Available from 1960s Programs

Delta Wing Aircraft	t B-58	F-4B	F-102	F-111*
Total Weight	163,000	43,588	31,263	90,453
Wing Group	12,156	4,538	3,000	8,400

Excepting B-58, Wing fraction ~10% of Total Weight.

What drives difference?

Materials, maximum g-levels, technology adapted?...

Examining hardware & performance uncertainties, Required wing weights to meet Mission requirements & thermal environments Currently among the least understood or defined.

Weight Estimation Process

Level 0 Estimate	Level 1 Estimate	Level 2 Estimate	Level 3 Estimate
impty Weight			
	Structure		-
		Wing	
		1.1.2	Skin
			Spars
			Ribs
			Stringers
		Fuselage	
		Empennage	
		Landing Gear	
	Propulsion		
		Bare Engine	
		Nacelle	4
	Systems		
		Electrical Equipment	
		Flight Controls	
		Avionics	3-1
	Interiors/Payload		
		Furnishings	
		Cargo Compartment	
Fuel Weight			
Payload Weight			
Crew Weight			

Spar s

- 1. resist bending and axial loads
- 2. form the wing box for stable torsion resistance



Ribs and Frames

- 1. Structural integration of the wing and fuselage
- 2. Keep the wing in its aerodynamic profile





Skin

reacts the applied torsion and shear forces transmits aerodynamic forces to the longitudinal and transverse supporting members

acts with the longitudinal members in resisting the applied bending and axial loads

acts with the transverse members in reacting the hoop, or circumferential, load when the structure is pressurized.

Stiffener or Stringers

- 1. resist bending and axial loads along with the skin
- 2. divide the skin into small panels and thereby increase its buckling and failing stresses
- 3. act with the skin in resisting axial loads caused

by pressurization.





Triton Systems LLC Houston TX 77058





This diagram's characteristics vary with alloy – and ambient temperature.

Alloy Characteristic	s Load	ed into "Wi	ngMod"	(e.g.	, See <u>v</u>	ww.m	atweb.co	<u>m & ww</u>	w.specialmeta	als.com)
Computer # ALLOY	Rho lb/cc	Stress ♂ Ultimate kpsi	Stress Yield kpsi	Elong Fract	Mod E Mpsi	Poisso Ratio	n Shear `Strength kpsi	∆σ _γ /∆tem Kpsi/º R	p ΔΕ/ΔΤ Mpsi/°R	Temp Range º R
1 Al-Li 2090 T84	.0936	76.10	68.20	.0500	10.00	.340	46.40 .	?		< 750
2 Al 2219 T6	.1030	55.00	37.00	.0200	11.00	.340		?		< 750
3 Al-Li 8090 T3	.1030	49.30	30.50	.1200	10.60	.340		?		< 750
4 Al-Li 8090 T81	.1030	63.80	49.30	.1300	11.20	.340		?		< 750
5 Ti6Al2Sn 1.5 Zn	.1630	151.00	136.00	.1900	16.70	.310		05		460 to1260
6 Ti8Al1Mo 1 V	.1580	171.00	155.00	.1700	17.40	.320		?		
7 Inconel 718	.2960	199.40	160.00	.2500	25.00	.300		0340	-0.004	460 to 960
8 Steel Maraging	.2890	150.00	110.00	.1800	27.60	.300		?		

Sample	Sample Calculations - Fixed Volumes, Number of Spars and Ribs												
Component # Name	Total Volume (in^3)	Alloy Code	Total Mass (lbs)	Alloy Code	Total Mass (lbs)								
1 Charc	11209 2	1		1									
I Spars	11298.2	T	1057.5	T	1057.5								
2 Ribs	12326.8	1	1153.8	2	1269.7								
3 Leading Edge	1425.9	1	133.5	5	232.4								
4 Skin	5705.9	1	534.1	1	534.1								
Total	30,757.8		2878.8		3093.7								

dE/dT & do_T/dT exist & <0.



Structural Analysis and Influence Coefficients for Delta Wings*

SAMUEL LEVY†

National Bureau of Standards

Summary

A method is presented for determining the stresses and deformations in delta wings of multispar construction having chordwise ribs and thin cover sheets. The spars need not be parallel, and the cover sheets can have large cutouts. The individual spars may be clamped, simply supported, or free at the root. The method is based on the interaction between the bending stiffnesses of the spars and ribs with effective cover sheet and the torsional stiffness of the cover sheet. The method is well suited to the use of high-speed computing machines. The method will be presented in a form particularly suitable for use with automatic digital computing equipment, since such equipment is finding increased use by aircraft companies. It is felt that the use of such equipment is imperative if the analysis time for highly redundant structures, such as delta wings, is to be kept low enough to allow several alternative configurations to be analyzed in a reasonable length of time.

Connor ny Course Curses

Levy, Samuel," "Structural Analysis and Influence Coefficients for Delta Wings*, *Journal of the Aeronautical Sciences*, Vol 20, July 1953, No. 3, pp. 449-454.



Premise of "Analysis of Low-Aspect-Ratio Aircraft Structures":



Many types of modern aircraft have low-aspect ratio (AR or λ) structural components.

Such structures cannot be treated satisfactorily by elementary beam theory; Consequently, more refined analyses are required.

Analytical procedures development at present (1960), however, restricted by 2 bounds.

1. Analysis of deformations & stresses need sufficient rigor to meet engineering accuracy demands;

2. Computer capabilities place upper limits on the degree of complexity of usable procedures. (Not necessarily a bad thing!)

An outgrowth of decade earlier work by Sam Levy at NBS referenced above. (e.g., integration of skin into cross rib and spar cross sectional stiffness)



Configuration Trade Candidates: 3 upper right of 7 suggested by Niu to adapt to Stellar-J double delta wing OML Employing varying Rib and Spar Numbers and Lengths.

Considerations: Spar Length (L_I) & Thickness in face of Sweep (Λ) and Taper (λ) Plus point or distributed loads (P_i) and cut-outs associated with engines and landing gear. **Constraints:** Weight budgets, Airfoil Dimensions, Material Strengths (E_I, I_I, σ_{YI}) in face of Aero-thermal, static and dynamic environments of flight.







Early 1950s Technology F-86 Structural Layout Swept wings With 2 or 3 Spars Ribs Perpendicular To Sweep



Argument against "Swept Spars": Deflection for loads indicated Grows to 3rd or 4th Power of beam length.

Nonetheless, swept spars Can benefit with bases near Wide portions of air foil.

	Max Shear	Max Moment	Max Deflection	Max Beam Slope
1	P/2	PL/4	PL ³ /48EI	$PL^2/16EI$
2	wL/2	$wL^2/8$	5wL ⁴ /384EI	$wL^3/24EI$
3	Р	PL	PL ³ /3EI	$PL^2/2EI$
4	0	М	$ML^2/2EI$	ML/EI
5	wL	$wL^2/2$	wL ⁴ /8EI	$wL^3/6EI$
6	$\frac{Pa}{L}$	$\frac{Pab}{L}$	$y_{\text{max}} = \frac{Pb(L^2 - b^2)^{3/2}}{9\sqrt{3}LEI}$ at $x = \sqrt{\frac{L^2 - b^2}{3}}$	$\theta_{\rm left} = -\frac{Pb(L^2 - b^2)}{6LEI}$
			$y_{\text{center}} = \frac{Pb(3L^2 - 4b^2)}{48EI}$	$ \theta_{\rm right} = \frac{Pa(L^2 - a^2)}{6LEI} $
7	$\frac{M}{L}$	М	$y_{\text{max}} = \frac{\sqrt{3ML^2}}{27EI}$ at $x = \frac{L}{\sqrt{3}}$	$\theta_{\text{left}} = -\frac{ML}{6EI}$
			$y_{\text{center}} = \frac{ML^2}{16EI}$	$\theta_{\text{right}} = \frac{ML}{3EI}$









Row Hierarchies Matter! Response to Sparse Matrices
Block Matrices behave like individual matrix elements
Matrix
$$\mathbf{A} = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$$
 Determinant Δ of $\mathbf{A} = ad-bc$
Matrix $\mathbf{A'} = \begin{bmatrix} \mathbf{A} & \mathbf{B} \\ C & \mathbf{D} \end{bmatrix}$ where $\mathbf{A} = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix} \mathbf{B} = \begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \end{bmatrix}$, et cetera.
 $\Delta & \mathbf{A'} = \text{Det} [\text{ AD-BC}]$
Matrix $\mathbf{A''} = \begin{bmatrix} \mathbf{A} & \mathbf{B} & \mathbf{C} \\ \mathbf{D} & \mathbf{E} & \mathbf{F} \\ \mathbf{G} & \mathbf{H} & \mathbf{I}^* \end{bmatrix} \Delta \mathbf{A''} = | \mathbf{A}(\mathbf{EI-HF}) - \mathbf{B} (\mathbf{DI-GF}) + \mathbf{C}(\mathbf{DH-GE}) |$

Off Diagonal Elements Block Elements either 0 or sparsely populated. * I not necessarily identity matrix. If C = G =0, Det A" = **|A(EI-HF)-BDI|** If C=G=H=F, Det **A"** = **|AEI|**



A(EI-HF)-B(DI-GF)+C(DH-GE)=AEI- BDI

R _{AI}	R _{BI}	M _{AI}	z _l (L _l)	R _{All}	R _{BI} I	M _{All}	z _{ii} (L _i	<i>)</i>	RAIII	R _{BIII} I	M _{AIII} z _{III} (L _{III})						1
(1)	(1)	(0)	(0)		F	2				C		R _{AI}		P ₁		0	
(0)	(1)	(0)	(k _{HI})			,	(-k ₋)		0	·	R _{BI}		P2		0	
(0)	(L _I)(1)	(0)	ļ								M _{AI}		P ₃		0	
(L _I 3/6	i) (0)	(L ₁ ²/2) (-E _l l _l)									Z _I (L _I)		P ₄		0	
				(1)	(1)	(0)	(0)					R _{AII}		P5		0	
	D)	(-k ₋)	(0)	(0)	(0)	(k _{HI}	-k _{II-III})		F	(k _{II-III})	R _{BII}		P ₆	_	0	
				(0)	(L _{II})	(1)	(0)					M _{All}	•	P7	-	0	
				(L _{II} 3/8)(0)	(L _{II} ² /2	2)(-E _{II} I	I)				Z _{II} (L _{II})		P ₈		0	
				 				(1)	(1)	(0)	(0)	R _{AIIII}		P ₉		0	
	Ģ	3		ļ	H	ł	ĺ	(0)	(1)	(0)	(k _{II-III})	R _{BIII}		P10		0	
								(0)	(L _{III})	(1)	(0)	M _{AIII}		P ₁₁		0	
								(L _{III} 3	/6)(0)	(L _{III} ² /2	2)(-E _{III} I _{III})	Z _{III} (L _{III})		P12		0	



 P_1, P_5, P_9 : Functions of point loads $P_{II} < a_L >$, unform loads $w_0 y < a_l >$, ramps $cy < a_l >$ etc,

P2: P6, P10: - 0 Loads associated with spring/rib reactive forces at points P1, at end of L1, L11, L11, ...

P3, P7, P11: Integration s of P1, P5, P9 to reflect moments at base point (A) for each spar, countered by reactive forces RA

 $P_4: P_8, P_{12}:$ Integrations from moment reliation, z deflections at end points, $Z_1(L_1), Z_{11}(L_{11}), Z_{111}(L_{111})$

Spars: Roman numerals I, II, III... Ribs: i, i+1, i+2...

Spring Constant k_{HI} i ith Rib stiffness between Spar I & II



P1 P5, P9: Functions of point loads P1i<a; >, unform loads w0y<a;>, ramps cy <a; > etc,

P2, P6, P10: = 0 Loads associated with spring/rib reactive forces at points P1, at end of L1, L11, L111.

P4: P8, P12: Integrations from moment rellation, z deflections at end points, ZI(LI), ZII(LII), ZIII(LIII)

P3, P7, P11: Integration s of P1, P5, P0 to reflect moments at base point (A) for each spar, countered by reactive forces RA

A(EI-HF)-B(DI-GF)+C(DH-GE)

=AEI- BDI

 $/ \text{Det TM} = z_I(L_I)$

Spars: Roman numerals I, II, III... Ribs: i, i+1, i+2...

Spring Constant k_{I-II} i ith Rib stiffness between Spar I & II



 $\Delta = \mathsf{E}_{|} \mathsf{I}_{|} \mathsf{E}_{||} \mathsf{I}_{||} \left[1 + \mathsf{k}_{|\cdot||} (\mathsf{L}_{||}^{3}/6 + \mathsf{L}_{||}^{2}\mathsf{L}_{|}/2) \right] - \mathsf{k}_{|\cdot||} \mathsf{E}_{||} \mathsf{I}_{||} (5/6\mathsf{L}_{||}^{3} + \mathsf{L}_{||} \mathsf{L}_{|}^{2}/2)$

Deflection z, Moment at A M_A , Reactive Forces at R_A and R_B

 $z_1(L_1) = \{ -E_{11} | I_{11} [P_4(1 - L_{11}^2 P_3) + (1/12 - 2/3P_3) P_1 L_{11}^5] + ... \}$

+ k_{I-II} [L_{I} (1 - P_{8} L_{II} [1+(1+ $P_{3}/2$) L_{II} + $L_{II}^{3}/6$ P_{1} +1/6(1- P_{3}) $L_{II}^{4}P_{4}$ + L_{II}^{5} $P_{1}P_{3}/12$]...

 $-P_8 (P_4/3 L_{II}^2 - 1/6 (P_1P_4 + P_3 + P_3P_4L_{II}^4 - P_1P_4L_{II}^7)) / \Delta$

 $\mathbf{z_{II}(L_{II})} = \{ -E_1 I_1 [P_8 - P_5 - P_7 L_{II}^2) - P_4 L_1^3 / 2 - P_4 L_{II}^2 / 2 \} / \Delta$

 $\mathbf{M}_{AI} = (\mathbf{L}_{I}^{2} + \mathbf{L}_{II}^{2})\mathbf{P}_{4} \{ \mathbf{E}_{II} \mathbf{I}_{II} [1 + \mathbf{L}_{II}^{3}\mathbf{P}_{3}(\mathbf{P}_{1} - 1)]$

 $-k_{\rm I-II}[1-L_{\rm II}^{3}/6(L_{\rm I}+L_{\rm II})P_{1}-2P_{3}+P1P_{3}P_{8}L_{\rm X}^{2}/2]\}/\Delta$

 $M_{AII} = E_1 I_1 E_{II} I_{II} P_7 / \Delta$

 $\mathbf{R}_{AI} = \mathbf{E}_{I} \mathbf{I}_{I} \mathbf{E}_{II} \mathbf{I}_{II} [\mathbf{P}_{1} + \mathbf{k}_{I-II} (\mathbf{P}_{1}\mathbf{P}_{8} + \mathbf{P}_{8})] / \Delta$

 $R_{BI} = -k_{I-II}E_{I}I_{I}E_{II}I_{II} / \Delta$



Spar Lengths $L_{I} = (y_{I1}-y_{I0})/\cos\Lambda_{I}$ $L_{II} = (y_{II1}-y_{II0})/\cos\Lambda_{II}$ "Numerical" or "Analytical"? 2 Cantilever Beams connected by Spring

Analogous to the first torque box of 2 Spars connected by 1 rib at their ends.

PRELIMINARY & PROVISIONAL BUT ILLUSTRATIVE



What about 3 Spars & 2 Ribs Analytical solution?





C:1.	Maxima (command line) – 🗖	×
x< [1., 1., 0., 0.,] <., 0.], [0., 1., 0., k], [0. [[[[[[[[, L1, 1., 0.], [L1*L1*L1/6, 0., L1*L1/2, -E*I]); 1 1 0 0] 0 1 0 k]	^
	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	
(%19) determinant(m) ;		
(%09)	$\frac{2 \operatorname{L1}^{3} \mathbf{k}}{3} = -\mathbf{E} \mathbf{I}$	
<%i10> determinant(m);	3	
(%010)	$\frac{2 \text{ L1}^{3} \text{ k}}{3} = - \text{ E I}$	
<pre><0. P1], [0., 1., 0., P2], [0 incorrect syntax: P1 is not a trix<[1., 1., 0. P1]</pre>	., L1, Ĩ., P3], [L1*L1*L1/3, O., L1*L2/2, P4]); n infix operator	
<0., P1], [0., 1., 0., P2], [0., L1, 1., P3], [L1*L1*L1/6, 0., L1*L1/2, P4]); [1 1 0 P1] []]	
(%011)	[0 1 0 P2] [] [0 L1 1 P3]	
(vil2) determinant(m1).	$\begin{bmatrix} 3 & 2 \\ L1 & L1 \\ & 0 & & P4 \\ 1 & 6 & 2 \end{bmatrix}$	
	2 3 3 L1 P3 2 L1 P2 L1 P1	
(%012) P4 -	2 3 6	
(%i13) _		~



Caveat:

Even with Sparse Block Matrices N grows large for series & factors.

Don't try this at home Without MathCad or similar tool. or Without annual license \$.

Note: Macsyma now available Via Source Forge... What about the deflection of segments as a function of **(T)** Element Temperature?

```
\frac{d\Delta}{dT} = \frac{d}{dT} \{ E_{I_{1}} E_{I_{1}} E_{I_{1}} [1 + k_{I_{1}} (L_{I_{1}}^{3}/6 + L_{I_{2}}^{2}L_{I_{1}}/2)] - k_{I_{1}} E_{I_{1}} [I_{I_{1}} (5/6L_{I_{1}}^{3} + L_{I_{1}}L_{I_{2}}^{2}/2)] \}
```

=($d\Delta/dEI$)(dE_I/dt)+ $d\Delta/dE_{II} dE_{II}/dt$

 $dz_{I}(L_{I})/dT = d/dT \{ \{ -E_{II} | I_{II} [P_{4}(1 - L_{II}^{2} P_{3}) + (1/2 - 2/3 P_{3}) P_{1} L_{II}^{5}] + ... + k_{I-II} [L_{I}(1 - P_{8} L_{III}^{2} [....])/\Delta \}$

=($dz_1(L_1)/dE_1$)(dE_1/dT)+($dz_1(L_1)/dE_1$)(dE_1/dT)

```
dz_{II}(L_{II})dT = d/dT\{\{-E_{I}I_{I}[P_{8}-P_{5}-P_{7}L_{II}^{2})-P_{4}L_{I}^{3}/2-P_{4}L_{II}^{2}/2\}/\Delta\}
```

=($dz_{II}(L_{II})/dE_{I}$)(dE_{I}/dt)+ $dz_{II}(L_{II})/dE_{II} dE_{II}/dt$

Spring or Rib Properties? $d\Delta/dk_{I-II} = \quad d\Delta/dk_{II-III} = ...$ Spar Length or Sweep... dz_I(L_I)/d L dz_I(L_I)/dT ...

....Pretty soon we are talking about optimization subject to constraints.



Chain Rule for Derivatives





		B. Long	itudinal dime	nsional deriva	tives
				Fligh	t condition
	1	2	3	4	5
h (ft)	0	θ	0	15,000	15,000
M ()	0.2	0.4	0.85	0.4	0.6
T_{π} (1/sec)	-0.001347	-0.000297	0	-0.000052	0.000225
X terp (1/sec)	-0.0813	-0.01558	-0.0308	-0.01476	-0.01288
Aircraft Descrip	tions	-0.01588	-0.0308	-0.01482	-0.01266
X_w (1/sec) Y_v ((f) (use 2) (mod)	-0.0312	-0.00379	-0.0308	-0.0371	-0.00588
X s [(fr/sec ²)/rad]	0.00432	0.00582	0.00769	0.00374	0.00414
Z = (1/sec)	-0.26	-0.1442	-0.1134	-0.1518	-0.1012
Phases/Modes	of Flight	t for 142	-0.1134	-0.1518	-0.1012
induce, incuce	-0.001681	-0.0022	-0.00382	-0.001385	-0.001616
$Z_{\rm m}$ (1/sec)	-0.307	-0.873	-2.23	-0.52	-0.818
Z_{δ} , [(ft/sec ²)/rad]	-7.07	-40.71	-188.0	-22.93	-56.92
$\mathbb{Z}_{\delta_T}[(\mathrm{ft/sec}^*)/\mathrm{rad}]$	0 1.0		0	0	0
1. Geometrical	& inert	lai Para	ameter	S -0.000467	-0.000407
M_u (1/sec-ft)	-0.0029	-0.000441	0.001108	-0.000468	-0.0004
2. Longitudina	l Dimen	sional [Derivati	Ve^{000482}	-0.000556
M* (1/2001). Or coloring	-0.0162	0.0101012	0.0502	-0.01338	-0.02
2 Latoral Dime	ncional	Doriva	tivos	-0.07	-19.49
J. Lateral Dime	0.000152	0.0001617	0.000243	0.0001181	0.0001309
1 Eleveter/Ele	vonlon	aitudin	0.000240	1 0.0001101	1
4. Elevalor/Ele	VON LOI	igituair	Idl	mercial parali	eters:
Transfer Fur	nction P	aramet	ters	Flight	eondition
5. Aileron Late	ral Tran	sfer Fu	nction l	Parame	ters
	0	c = 0	0	15,000	15,000
6. Rudder Late	ral Iran	ster Hul	nctions	0.4	0.6
a (ft/see)	1116	1116	1116	1057	1057
7 Lateral Cour	ling Nu	merato	ors (Two	Contro	S1001496
V _{Te} (ft/sec)	0 223	1110101417	950	423	634
$\bar{q} = \rho V^*/2 \text{ (lb/ft*)}$	59.2	237	945	134	301
117 - 116 7	22,058	17,578	17,578	17,578	17,578
14 (16)		.046	946	046	040
m (rb) m (slugs)	658	11.11.1.1	D PATER	8.1000	S 11000
m (slugs) I_x (slug-ft ²) I_z (slug-ft ²)	658 16,450 20,200	8,010	8,070	8,190	8,000
$m_{\rm f} ({\rm slugs}) \\ I_x ({\rm slug} \cdot {\rm ft}^2) \\ I_y ({\rm slug} \cdot {\rm ft}^2) \\ I_{\rm const} ({\rm slug} \cdot {\rm ft}^2) $	658 16,450 29,300 35,220	8,010 25,900 20,300	8,070 25,900 29,220	8,190 25,900 29,140	8,000 25,900 29,300
$m (slugs) I_x (slug-ft2) I_y (slug-ft2) I_z (slug-ft2) $	658 16,450 29,300 35,220 -5 850	8,010 25,900 29,300 -446	8,070 25,900 29,230 1,159	8,190 25,900 29,140 -1,994	8,000 25,900 29,300 37
$m (16)$ $m (slugs)$ $I_x (slug-ft^2)$ $I_y (slug-ft^2)$ $I_{xz} (slug-ft^2)$ $I_{xz} (slug-ft^2)$ $r_{xz} = lc$	658 16,450 29,300 35,220 -5,850 0,25	8,010 25,900 29,300 -446 0.25	8,070 25,900 29,230 1,159 0,25	8,190 25,900 29,140 -1,994 0,25	8,000 25,900 29,300 37 0,25
$m (slugs)$ $I_x (slug-ft^2)$ $I_y (slug-ft^2)$ $I_{xz} (slug-ft^2)$ $I_{xz} (slug-ft^2)$ $x_{xyz} (clug-ft^2)$ $x_{xyz} (clug-ft^2)$	$ \begin{array}{r} 658 \\ 16,450 \\ 29,300 \\ 35,220 \\ -5,850 \\ 0.25 \\ 19.5 \end{array} $	8,010 25,900 29,300 -446 0.25 4.7	8,070 25,900 29,230 1,159 0.25 0,4		8,000 25,900 29,300 37 0,25 3,4

Table A-3 (Continued)

Design Activity	BA	BB	BC	BD	BE	BF	BG	BH	BI	BJ	ВК	BL	BM	BN	BO	BP	BQ
		primary	units	units	w/o glove					1	1	1			18/7		
Stellar-I Descriptions		Sref wing	rft2	h2	1317	1317	1317	1317	1317	1317	1317	1317	1317	1317	1317	1317	1317
Stellar 3 Descriptions		bspan	ft2	ft2	70	70	70	70	70	70	70	70	70	70	70	70	70
		Crichord	inches	inches	490	490	490	490	490	490	490	490	490	490	490	490	490
		Lt chora	inches	Inches	0.1469	0 1469	0 1469	0.146939	0 1469	0.146939	0.14694	0.1469	0 146939	0 14694	0 14694	0.14694	0.1469
Phases/Modes of Flight for		sweep Le	dea	dea	45	45	45	0.140333	45	45	45	45	0.140333	45	45	45	45
		sweepLe	deg	deg	0	0	0	0	0	0	0	0	0	0	0	0	0
		C bar m	_	inches	332.82	332.82	332.82	332.8161	332.82	332.8161	332.816	332.82	332.8161	332.816	332.816	332.816	332.82
1. Geometrical &		9			32.174	32.174	32.174	32.174	32.174	32.174	32.174	32.174	32.174	32.174	32.174	32.174	32.174
Inartial Paramotors		pi			3.1416	3.1416	3.1416	3.141593	3.1416	3.141593	3.14159	3.1416	3.141593	3.14159	3.14159	3.14159	3.1416
mertial Parameters		Second	lary	1.0													
		horizonta	altail	ht2	0												
		elevon		112													
2. Longitudinal Dimensional Derivatives		elevator		dt2									4				
		rudder		612 ft2										-			
		speed br	ake	ft2			- I I	Jnder	Cons	structi	on		-	-			
3. Lateral Dimensional Derivatives		body flap)	ft2													
1 Elevon Longitudinal	Aircraft	Stellar-	J 35	name	Nominal fl	ight							5	1-			
4. LIEVOIT LONgituumai	Paramet	ers															
Transfer Function Parameters	iumber	name		units	0	1	2	3	4	5	6	7	8	9	10	11	12
	EA BE BEC BF BI BI <t< td=""><td></td><td></td><td></td></t<>																
	0	Ь	span	ft													
5 Aileron Lateral Transfer	0		chord m	∈ft													
J. Ancion Edicial Indusici	0	gammaU	ipa _b	deg		0	10000	25000	25000	45000	0000	100000	70000	45000	25000	5000	
Function Parameters	2	n Maak	ait	rc		03	0.7	25000	0.85	40000	12	35	25	45000	25000	0.5	0.2
	3	Plach	sound	fos		1116.7	1077.4	1016	973.14	80.836	968 18	3.5	2.J 968 18	973.14	1016	1097.1	1116.7
	4	rho	densitu	slua/ft3		0.0024	0.0018	1.07E-03	0.0007	4.62E-04	2.26E-04		1.40E-04	4.62E-04	1.07E-03	2.05E-03	0.0024
6 Rudder Lateral Transfer Functions	5	Vt0	tanyelo	fps		335.01	754.18	812.8	827.17	871.272	1161.82	0	2420.45	1167.77	914.4	548.55	223.34
	6	q	dynamic	b/ft2		133.44	499.28	352.2223	252.47	175.458	152.266	0	409.8954	315.195	445.781	308.234	59.308
	Engir	ne Trade	es S	tandard	Atmos	Qua	rtic Roo	ts R.	🕀	: •							

Lateral Coupling Numerators (Two Controls)

Many aerospace publications similar to McRuer, Ashkenas and Graham's **Aircraft Dynamics & Automatic Control**, but this is a particularly thorough treatment of linear theory with an abundance of aircraft illustrations.

Search on line indicates that NASA Ames and other agencies in the 60s-70s' examined 50-100 aircraft in detail. In addition to control – structural design.

The charts provide

- 4th order longitudinal & lateral transfer functions, plus
- Selected c ontrol response features (open or closed loop).

Also

- Approximate solutions for 4 sets of roots with varied natural frequencies & damping (or lack thereof).



$$F=F_{\mathrm{ext}}-kx-crac{\mathrm{d}x}{\mathrm{d}t}=mrac{\mathrm{d}^2x}{\mathrm{d}t^2}.$$

When no external forces are present (i.e. when $F_{ext} = 0$), this can be rewritten into the form

$$rac{\mathrm{d}^2 x}{\mathrm{d}t^2}+2\zeta\omega_0rac{\mathrm{d}x}{\mathrm{d}t}+\omega_0^{\ 2}x=0,$$

where

$$\omega_0 = \sqrt{\frac{k}{m}}$$
 is called the 'undamped angular frequency of the oscillator' and

$$\zeta = \frac{c}{2\sqrt{mk}}$$
 is called the 'damping ratio'.

The value of the damping ratio ζ critically determines the behavior of the system. A damped harmonic oscillator can be:



Dependence of the system behavior on the value of the damping ratio ζ



The "classical" theory of aircraft dynamics in cruise flight identifies

4 Basic Systems of Harmonic Oscillators in

2 sets of separable Differential Equations (approximated by constant coefficients) revised for phases of flight.

- Longitudinal: Pitch (θ), Axial (X) and Normal (Z) motions Providing Harmonic Oscillator Roots for Phugoid and Short Period
- Lateral : Roll (φ), Yaw (Ψ) and Side (Y) motions
 Providing Harmonic Oscillator Roots
 Dutch Roll
 Secondary

In Other Words: Stability and Control Analysis is A Way of Surveying Overall Design

Simpler and More Complex Systems Can Be Derived for Special Flight Regimes (Coast and Accelerated).

Roots are derived from Mass Properties (Inertia Tensor, Aerodynamics and Equilibrium Forces Controls are sized and modulated in forcing functions with System Dynamics analysis. But to obtain the values which provide the roots, we need to compute, measure or estimate a host of vehicle features which change during flight (sector the results)

There is joy in the house each time One of those entries is obtained – especially when A derivation method is obtained as well.

Solution to the "handling problem" serves as evidence of a cumulative effort crossing several design disciplines:

- Aerodynamics,
- Structures,
- Mass Properties,
- -Propulsion,
- -Thermal
- Flight Performance.



Also, we need to evaluate solutions obtained in light of mission requirements, cost, efficiency &risk. ... Now why do this at all?



With Roots of the Longitudinal and Lateral Dynamics Evaluated for Flight Segments (Phases or Major Modes)

Beside Jet & Rocket Engines, Aerodynamic Control Effectors Include:
A & B)Elevons for Pitch and Roll (Y and X axes), inboard & outboard respectively
C) Vertical Tail Rudders for Yaw (Z axis), outboard winglet rudders (TBD) D).
Body flap(E), elevon and split rudder initial settings for "trim" for flight phase or major mode.



Stellar-J Flight Control



Stellar J Defined as a rigid body With changing Center of Mass

$$\mathbf{R} = rac{1}{M}\sum_{i=1}^n m_i \mathbf{r}_i,$$

Changing Moments & Products of inertia

$$egin{aligned} I_{11} &= I_{xx} = \left(\sum_{k=1}^N m_k \left(y_k^2 + z_k^2
ight)
ight), \ I_{22} &= I_{yy} = \left(\sum_{k=1}^N m_k \left(x_k^2 + z_k^2
ight)
ight), \ I_{33} &= I_{zz} = \left(\sum_{k=1}^N m_k \left(x_k^2 + y_k^2
ight)
ight), \ I_{12} &= I_{21} = I_{xy} = -\left(\sum_{k=1}^N m_k x_k y_k
ight), \ I_{13} &= I_{31} = I_{xz} = -\left(\sum_{k=1}^N m_k x_k z_k
ight), \ I_{23} &= I_{32} = I_{yz} = -\left(\sum_{k=1}^N m_k y_k z_k
ight). \end{aligned}$$







Center of Gravity Management in Flight Includes System of Baffles & Propellant Transfer
Overall Layout



Modularity: Wing Elements Plan to Trade Out: - Airfoil, -Leading & Trailing Edge Sweep, -Root & Tip Chord, - Main Spars, Ribs, Cut-Outs & Flaps NACA 64-208 (naca64208-il) NACA 64-208 - NACA 64-208 airfoil Air Foil NACA 64-208 Internal Layout Guide 30 25 20 15 -10 -15 -20 50 450 500 0 100 150 250 300 350 400

unit or inch

x unit or inche



Based on Mission or Development Phase Expendable Upper Stage System IIA & IIB Vary in Diameter, Length & Mass As with Aircraft Capacities for AvGas Load for Range Upper Stage Weight Matched to Mission Requirements









Space Shuttle Orbiter Aero Applied to Stellar-J





Orbiter CG Limits Entry Interface, M=3.5, & Touch-Down 1076.7 to 1109.0 inches (32 inches) Abort (RTLS) & Post ET-Sep 1079 to 1109

Sample Pre-Flight (1990) Estimates*									
Nominal	F35	F37	F39	F40					
ET Sep	1106.3	1116.5	1110.4	1100.3					
EI	1081.8	1090.8	1082.0	1087.4					
M=3.5	1080.5	1089.3	1080.4	1079.7					
TD	1081.9	1090.9	1081.8	1081.1					

Orbiter Length = 1365 inches 2/3L = 910 X₀ = **1145 inches** Nominal Moment arm: 36" to 69"

How do dispersions affect control surface trim?

*Shuttle Systems Weight and Performance NTSTS-09095097, June 19, 1990, NASA JSC











Jet Engine Trades Rolls Royce & Other Candidates Images, Parameters & Analysis Methods

Select the Best Jet Engine (Combination) for Stellar-J Configuration & Mission

Based on Performance, Constraints, Costs,

Using Saaty's Analytical Hierarchy Procedure (AHP)

Analogous to a Family Selecting a New Car









Engine Data : Two Engine Trades - Gulfstream IV/450 Baseline to allow margin for drag

Name Type 		Spey 511-8 Axial Flow Fan	Tay 611 8C Axial Flow Fan	BR 700-710 Axial Flow Fan
Dry Wgt – Tail Pipe	(lbs)	2483	2951	3520
Max Length	(inches)	110	95	87
Max Diameter	(inches)	32.5	44	52.9
Overall Pressure Ratio at Max Power		18.4	15.8	25.5
SFC at Max Power		0.8	0.69	0.39
Bypass Ratio		0.6	3.2	4.0
Max Power at Sea Level Thrust (lbf)		11,400	13,850	14,000-17,000*
Combustor Type		Can-Annular	Can-annular	Annular
Number of Turbine Stages(Low, High Pressure)		2,2	2,3	2,2
Number of Fan Compressor Stages		5,12	1,3,12	1,12
Application		Gulfstream II&III	Gulfstream IV/450	Gulfstream V/550
Max Cruise (knots/mach)		500	488	?
Max altitude	(ft)	45,000	45.000	51,000

* 15,385 lbf with G-550



Jet Engine Selection Similar, but Different

 Capability to deliver High altitude with heading Speed to reduce Delta V.
 Weight of Engine
 Fuel Consumption
 Range after Satellite
 Deployment
 Cost per Unit.
 Reliability (Re-Start)
 Operating Life
 Inter-Related? ... Yes.

Weight and normalization?



Market Research

For 21 years Utah State University has hosted the Small Satellites Conference

A 2007 Summary:

62 exhibitors included

- satellite & component vendors, satellite users,
- large and small aerospace companies,
- university, government & private research units domestic and foreign
- 78 presented papers represented with 137 cited organizational units



Cicero Spacecraft

-Broad Reach Engineering reported on CICERO: a constellation of 100 30- kg satellites. CICERO will perform radio occultation measurements of earth's atmosphere for weather and hurricane prediction. Discussions with the vendor about this 3rd generation project indicates: Hardware is in assembly, but no launcher is signed on for deployments over the next decade.

- World small satellite leader Surrey Satellite Center (UK) described several similar prospective programs. About a dozen universities reported on individual satellite programs...

Annual satellite launch rates (monitored by Futron Research) do not match systems introduced. Satellite backlogs (~500) with introduction of new satellite concepts would go even higher. But some waiting for launch slots or low cost opportunities will eventually fade away; Research and development teams, organizations and sponsors will eventually move on -Unless more rapid, lower cost means of satellite launch are made available. The need for such a launch system is a recurring conference theme.



Satellite Market

In 2004 Triton Identified 8 Primary Markets for 4 Vehicle Systems

Vehicle Types and Configurations								
LEO Satellite Payloads (lbs):	100-200	1,000	2,000	10-20,000	-			
	\mathbf{A}	В	С	D				
Mission Model for Revenue	Demo	35-ton	70-ton	350-ton	+ Orbiter			
1. Sounding Rockets	x	x						
2. Sub-Orbital Tourism	?	X	x					
3. Micro-Satellites	X	X	x					
4. LEO Satellite Constellations	X	X	x					
5. LEO Space Platforms				x				
6. Rendezvous Payloads		X	x	x	x			
7. Sortie and Return Payloads		x	x	x	x			
8. Rescue Standby		x	x	x	x			

Primary Markets Missions (1-8 and Subsets) Graded on Scale of 1 –5 with 8 Parameters

(Red X: High return on low initial investment)

Market Maturity
 Market Demand
 Price Margin over Mission Cost
 Potential Volume

- 5. Mission Procedural Complexity 6. Mission Hardware Complexity
- 7. Regulatory Barriers
- 8. National Economic &/ Strategic Security



Backup Notes



Moe Miller would often tell us Project issues boiled down to Performance, Schedule & Cost **POST2 (History)** was developed from the original POST software starting in 1995 - the 2006 NASA Software of the Year Runner-Up.

POST development began in the early 1970's in partnership with the Martin Marietta Co. as a space shuttle simulation program. ..Improved with capabilities added w.r.t.

vehicle modeling, trajectory simulation, targeting and optimization.

Considerations Here for Constrained/Iterated Paths of Defined Vehicles Not Constrained /Iterated Vehicle Designs

3- and 6-DOF POST can optimize & target ascent, entry, and orbital trajectories since the early 80's.

The ability to analyze only one vehicle within a single simulation is insufficient to properly study advanced launch vehicle concepts such as a multi-stage to orbit vehicle with fly-back boosters. (....???)

Traditionally POST users had to do several trajectory simulations and optimize the problem external to POST.

POST II can solve this problem within a single trajectory simulation.

Example: determining where launch vehicle expended stages or jettisoned portions of entry and orbital vehicles impact the attracting body while including the primary vehicle in the simulation permits faster evaluations such as is **necessary to support spacecraft and launch vehicle operations.**



Deflection
$$y(x) \coloneqq y_1 + \theta_1 \cdot x + \frac{M_1 \cdot x^2}{2 E \cdot I_x} + \frac{R_1 \cdot x^3}{6 E \cdot I_x} \downarrow$$

 $-(x > a) \cdot \left(\frac{W}{6 E \cdot I_x} (x - a)^3\right)$
Moment $M(x) \coloneqq \left(\frac{d^2}{dx^2}y(x)\right) \cdot E \cdot I_x$
Shear $V(x) \coloneqq \left(\frac{d^3}{dx^3}y(x)\right) \cdot E \cdot I_x$

For the segments of Spars & Ribs, Loads we will refer to generally as P_{1} , P_{2} , P_{3} ,...

Forces applied at specific spar or rib points Represented by "Singularity Functions" at point "a"

Uniform loads begin at "a" and end at "b"

Same true of ramped and other functions.

In force, moment & deflection equations, Integrated & differentiated as implied.







5



Introduction



On September 4, 2013 in an auditorium adjacent to the NASA JSC, The directors of Houston Airports, Rice University's Space Institute and 6 former astronauts representing commercial space firms Met to speak with the public about space enterprise.

"Rice Space Institute, Houston Airports, Bay Area Houston Economic Partnership (BAHEP), Commercial Spaceflight Federation (CSF) and 5 Firms Present Panel Discussion on Commercial Spaceflight and a Spaceport"



Ironically, it was one of the 6 astronaut speakers (Chris Ferguson) Whose duty it was to call in the last report from a Space Shuttle flight deck: "Houston, wheels locked." after Shuttle Atlantis mission STS-135 landed at KSC on 21 July 2011.

Yet despite the retirement of the Space Shuttle, the director of the Houston Airport System chose this evening to promote Elliington Field, Houston's "3rd Airport" as a Spaceport.



Mr. Diaz, in assessed the current commercial space industry as a \$256 billion global enterprise with a growth rate ~5% annually.

And despite the gathering of space businesses, None addressed operations at Houston-Ellington Nor the most accessible services, identifiable customers or markets!

WE WILL.

NOTES

Development Snap Shot

- As the Design Matures, Useful Engineering Textbooks Include...
- Other Areas Not Well Documented (Ascent Trajectories, Especially Air-breathing)
- Delta Wings (more and more cantilever and intersecting spars and ribs) though structures books abound.
- Current Effort Defining Aircraft Dynamics & Control through Major Modes

History HTOL Launch and Related Matters – from Our Perspective

- Due to my age, I discovered spaceflight before Star Wars..

Captain Video, Tom Corbett – Space Cadet, Sputnik and Robert Heinlein...

Why Do This and What Do Customers Want?

Consider Professor Van Allen of Iowa State Pioneer of Spacefligtt with Explorer I

To read his opinion pieces, the only reason to build a rocket is to study magnetospheres...

At the other extreme are friends and colleagues of Elon Musk, they are preparing to settle Mars.

Analysis Topics

-Trajectories with and without Wings

- -Performance Analysis
- Jet engines, wings, effective ISP and the removal of DV (principally work) from the rocket equation
- -Reusable Systems, especially propulsion (do or can they pay for themselves)
- Lessons or data from previous programs (Shuttle and its derivatives Liquid Booster Engines, aero, conventions)
- The X-34, the little reusable that never flew.